

Experimental data: s-values & helical propensities

Table 2. *Helix propensity values measured at 273 K*

Residue	s-Value ^a	w-Value ^a	$-RT\ln(w)$ (kcal/mol)	$\Delta\Delta G^0$ (kcal/mol)
Ala	1.54	1.61	-0.258	-1.88
Arg ⁺	1.1 ^f	1.2 ^f	-0.047	-1.67
Leu	0.92	0.96	0.022	-1.60
Lys ⁺	0.78	0.82	0.108	-1.52
Glu ⁻	0.63 ^b	0.66 ^b	0.225	-1.40
Met	0.60	0.63	0.251	-1.37
Gln	0.53	0.56	0.314	-1.31
Glu ⁻	0.43 ^b	0.45 ^b	0.433	-1.20
Ile	0.42	0.44	0.445	-1.18
Tyr	0.37-0.50 ^c	0.39-0.53 ^c	0.344 ^c -0.511	-1.28 ^c to -1.11
His ⁰	0.36 ^d	0.38 ^d	0.525	-1.10
Ser	0.36	0.38	0.525	-1.10
Cys	0.33	0.35	0.570	-1.06
Asn	0.29	0.31	0.635	-1.00
Asp ⁻	0.29 ^e	0.31 ^e	0.635	-1.00
Asp ⁰	0.29 ^e	0.31 ^e	0.635	-1.00
Trp	0.29 ^c -0.36	0.30 ^c -0.38	0.525-0.653 ^c	-1.10 to -0.97 ^c
Phe	0.28	0.29	0.672	-0.95
Val	0.22	0.23	0.797	-0.83
Thr	0.13	0.14	1.07	-0.56
His ⁺	0.06 ^d	0.06 ^d	1.53	-0.10
Gly	0.05	0.05	1.62	0
Pro	≈0.001	≈0.001	≈4	>5

Chakrabartty, Kortemme, Baldwin, Protein Sci 1994

Measured from fit of theory to host-guest measurements

allows now the **prediction** of the helicity of a given amino acid sequence

^a Values obtained by applying Lifson-Roig theory modified to include either N-capping or charged group-helix macrodipole interactions. Conditions: 273 K, 1.0 M NaCl for uncharged residues and Lys, and 273 K, 10 mM NaCl for Arg, Asp, Glu, and His.

^b Values from Scholtz et al. (1993).

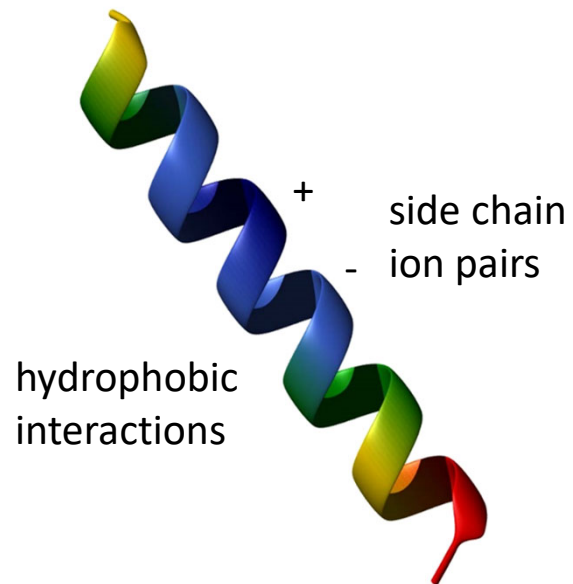
^c Values corrected for error in fraction helix measurement caused by aromatic contribution.

^d Values from Armstrong and Baldwin (1993).

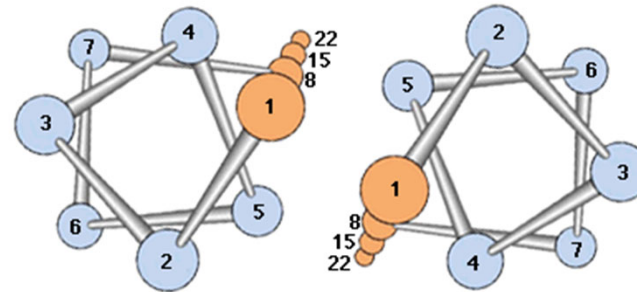
^e Values from Huyghues-Despointes et al. (1993).

^f Values from Huyghues-Despointes and Baldwin (unpubl.).

Side chain interactions: Stabilizing and destabilizing



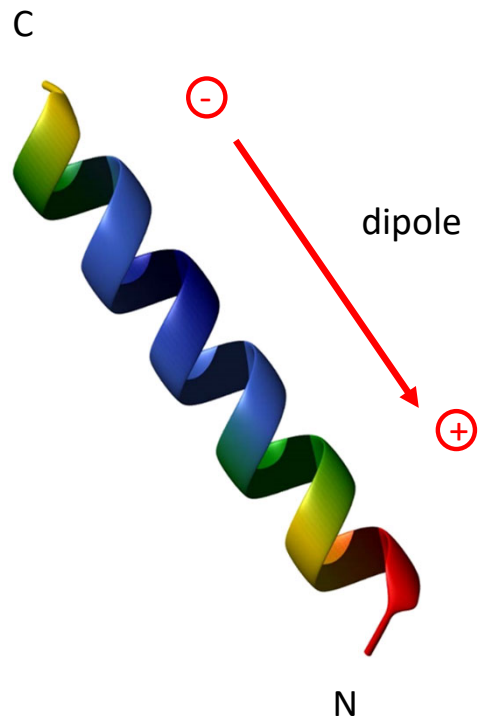
The helical wheel:



Mapping side chains on the same face of the helix

interactions possible
stabilizing or destabilizing

Interactions with the helix-dipole



Negative charges at the
C-terminus

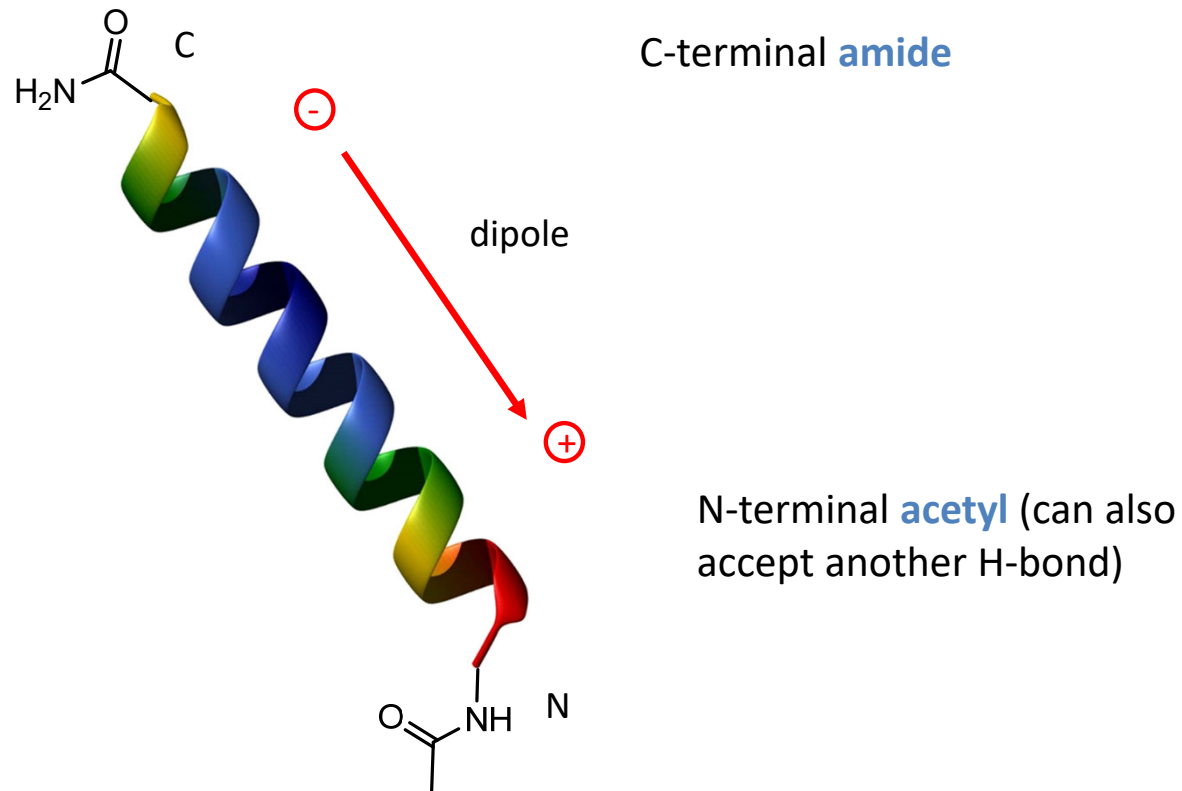
or

positive charges at the
N-terminus

destabilize helices

Capping groups can overcome this effect

Capping groups in isolated helices



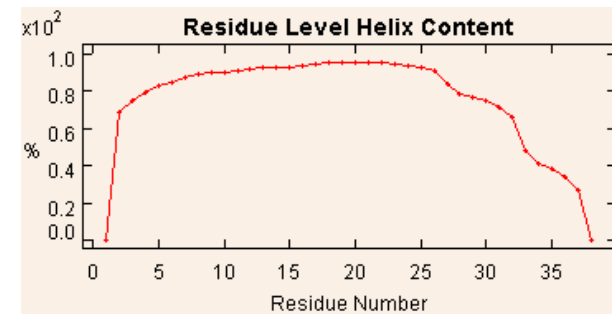
Helix prediction: AGADIR

Secondary structure prediction based on helix-coil theory

takes into account further empirical parameters

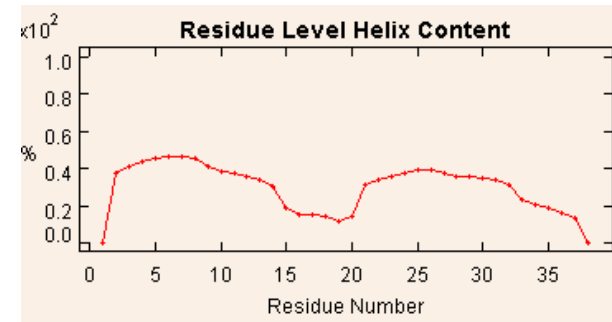
Peptide 1

AAAAAAAAQQAAAAQWAAA
AAAAAAAAQQAAAAQWAAA



Peptide 1

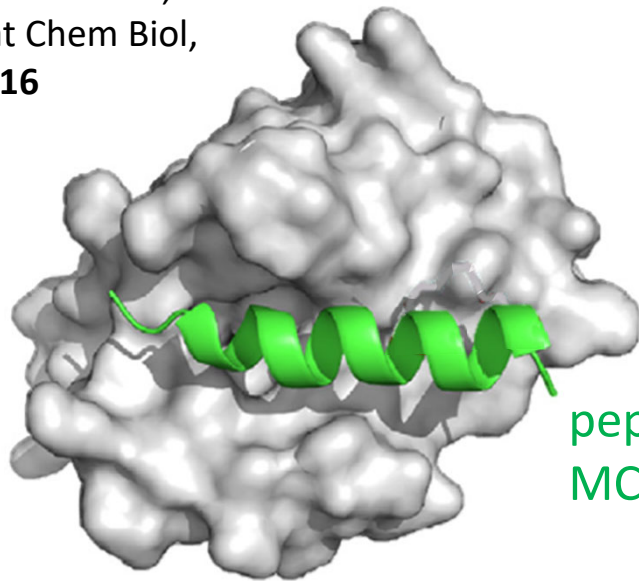
AAAAAAAAQQAAAAQWAGG
AAAAAAAAQQAAAAQWAAA



Muñoz, V. & Serrano, L. (1994a),
Nature: Struct. Biol. 1, 399-409

How to stabilize helix enough to make an efficient drug?

Stewart et al,
Nat Chem Biol,
2016



peptide from BCL-2, a
MCL-1 binding partner

MCL-1: resistance factor in
human cancer → prevents
apoptosis of cancer cells

Targeting protein-protein interactions:

- very difficult with small molecules
- peptides are a possible solution

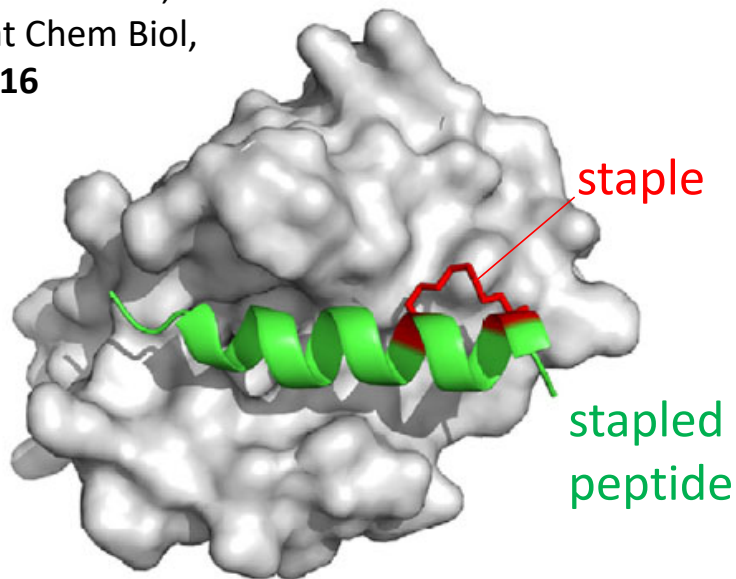
→ Problems:

structural stability, cell
permeability, stability to proteases

→ Solution: peptides with
stabilized structure (α-helix)

Approach: 'Stapling' the peptides

Stewart et al,
Nat Chem Biol,
2016



MCL-1: resistance factor in human cancer → prevents apoptosis of cancer cells

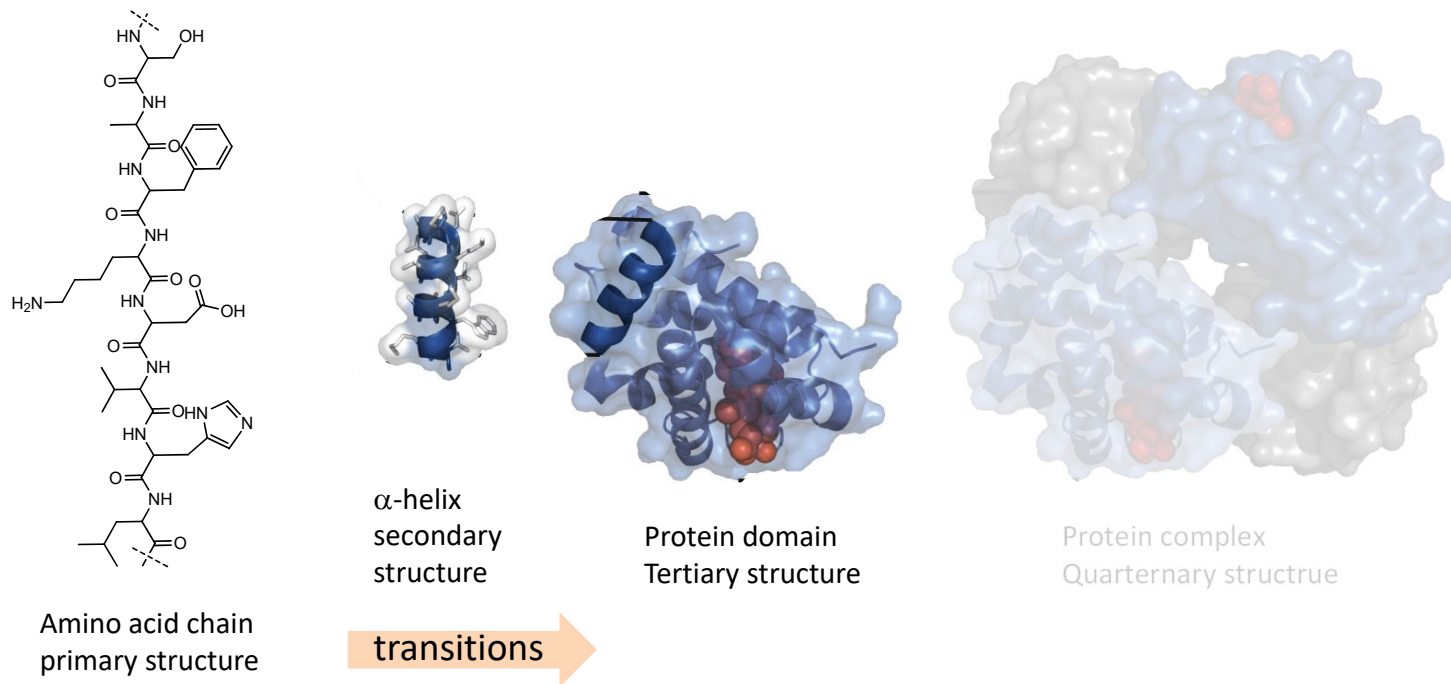


- synthesis via ring-closure metathesis
 - strong increase in helicity → why?
 - better cell permeability and serum stability
- drug like properties possible

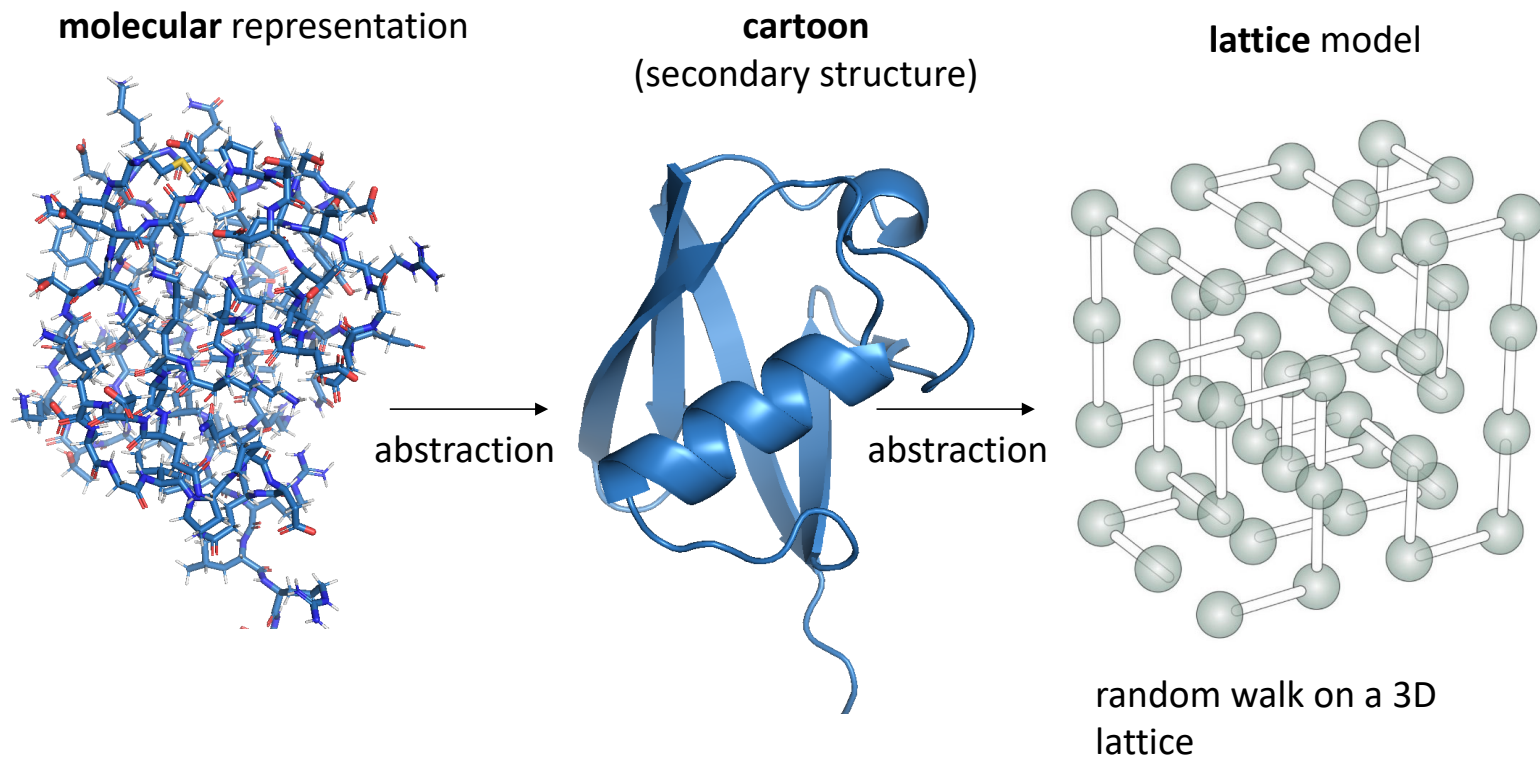
Summary

- Using simple assumptions and statistical thermodynamics the cooperative conformational change from coil to helix can be analyzed
- The cooperativity of the transition depends on the nucleation parameter σ
- Experiments produced values of the elongation parameter s for all amino acid residues, these serve as a predictor of helix stability
- Charges at helix termini stabilize the helix if they favorably interact with the helix dipole, otherwise they weaken the helix
- Capping motifs stabilize helices through hydrogen bonding with termini, optimal charges, conformations

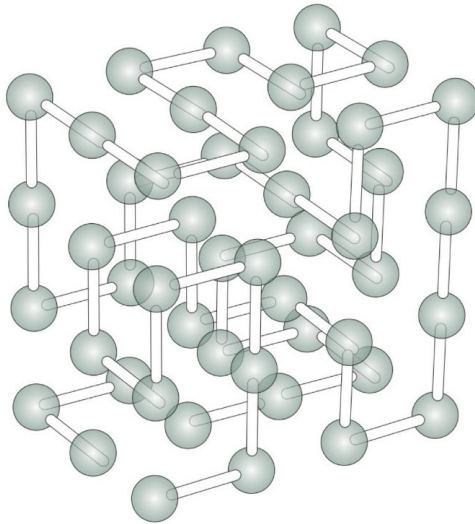
Proteins – Structural hierarchy



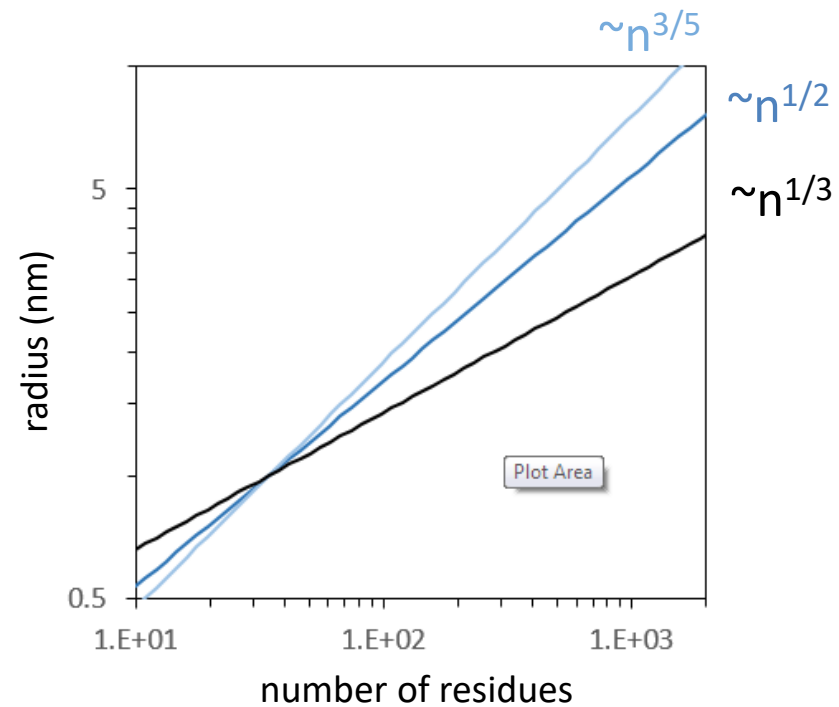
Protein organization in 3D



Scaling laws for protein size

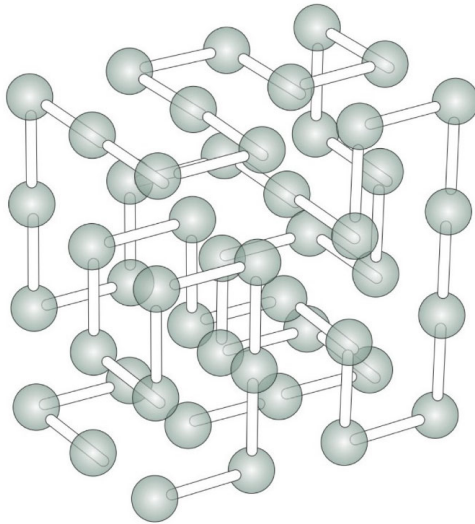


Scaling laws for a random walk
self-avoiding chain: $r \sim n^{3/5}$
random chain: $r \sim n^{1/2}$
compact chain: $r \sim n^{1/3}$

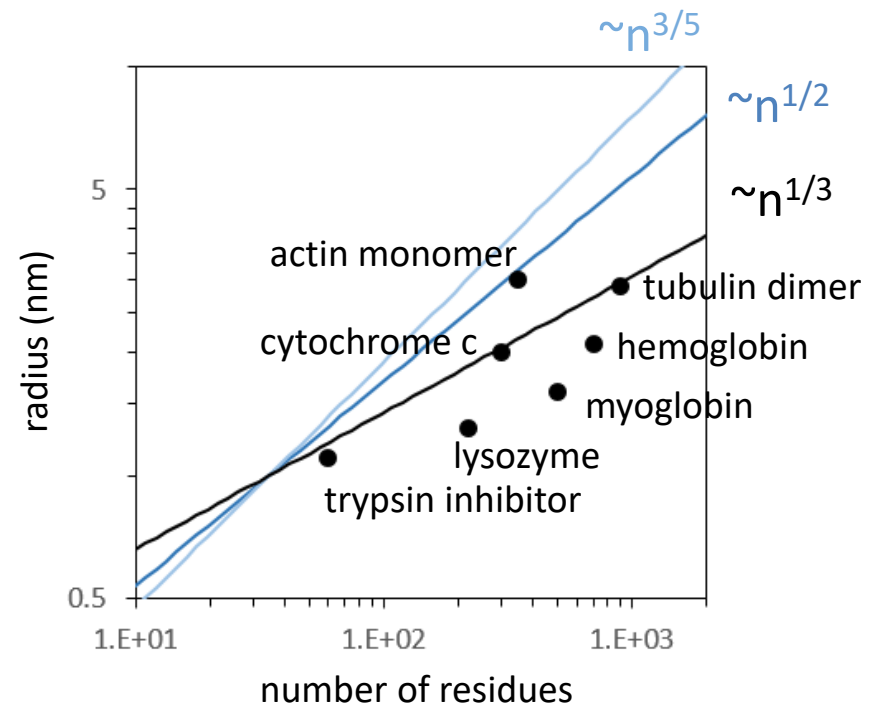


Adapted from Physical Biology of the Cell (Chapter 8)

Scaling laws for protein size



Scaling laws for a random walk
self-avoiding chain: $r \sim n^{3/5}$
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Adapted from Physical Biology of the Cell (Chapter 8)

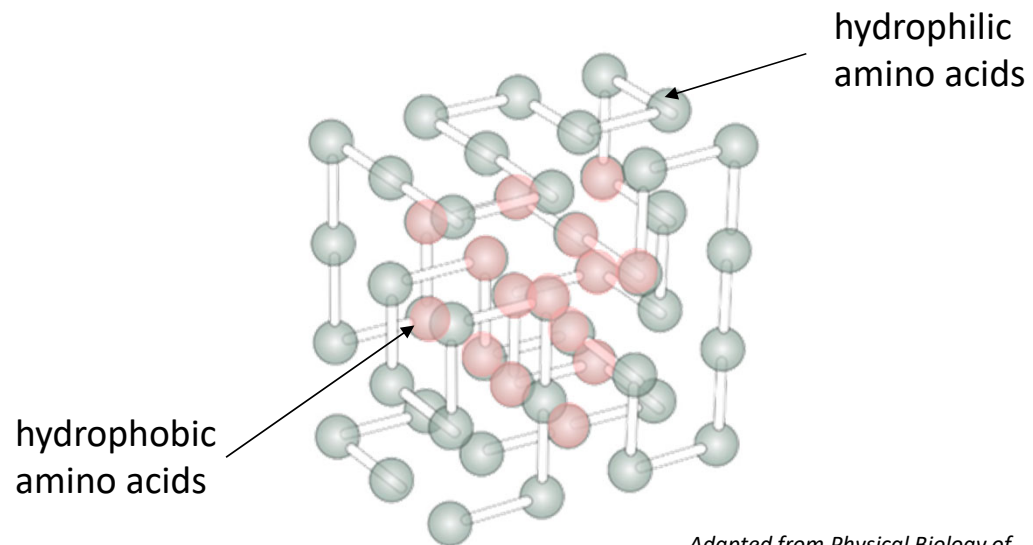
How does a protein find its native state?

Random search:

Even on a lattice (6 degrees of freedom) 100 aa protein has $6^{100} = 6.5 \times 10^{77}$ conformations, random search would take astronomical amount of time

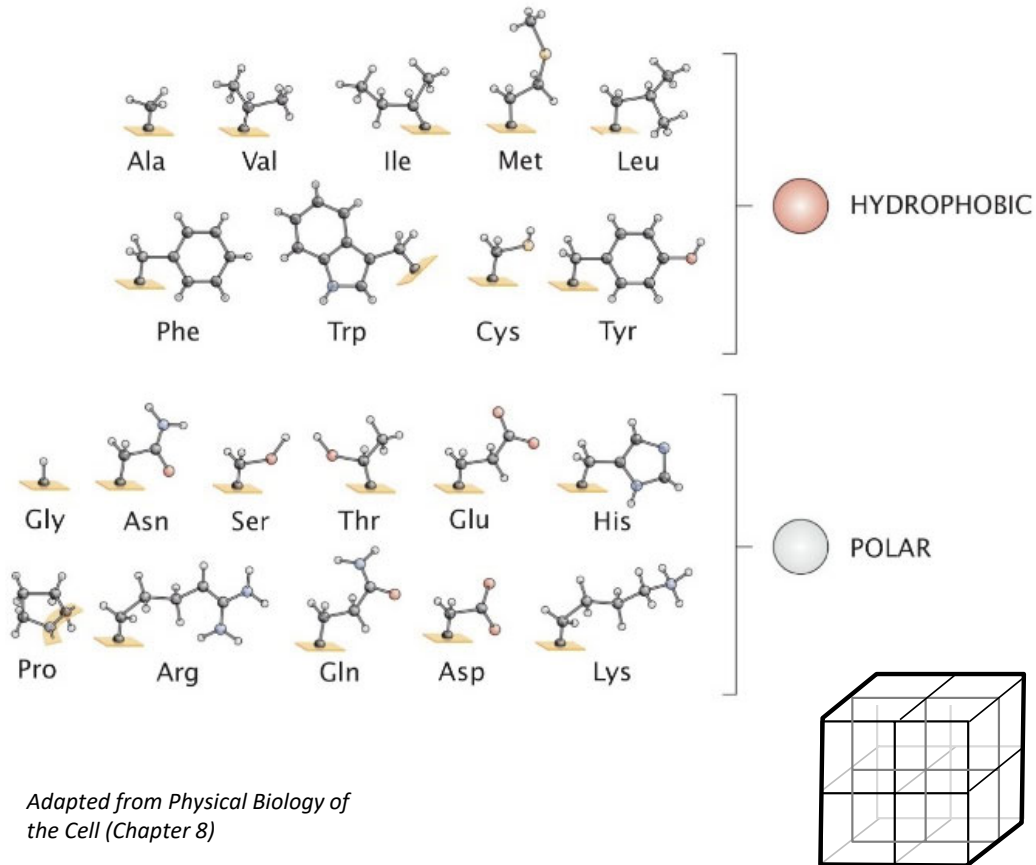
Mechanism:

Hydrophobic collapse



Adapted from Physical Biology of the Cell (Chapter 8)

HP-models of protein folding



Adapted from Physical Biology of the Cell (Chapter 8)

categorization of amino acids as **hydrophobic (H)** or **polar (P)**

→ 2 letter alphabet allows an abstract model of structure formation

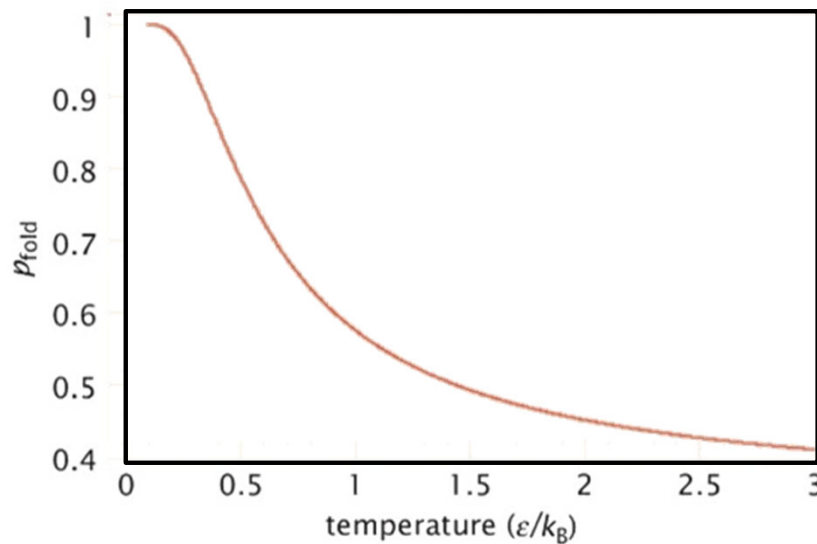
Of note: finer categorization possible -> charged, acidic, basic, helix forming, etc.

Quiz: How many HP sequences possible on a 3x3x3 lattice?

How many different HP protein configurations are possible?

Note: there possible 103'346 compact structures.

Temperature dependence of folding



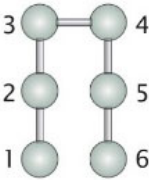
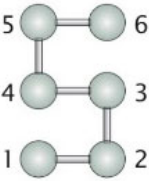
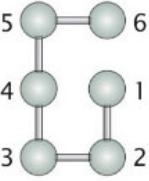
$$p_{\text{fold}} = \frac{e^{-2\beta\epsilon}}{e^{-2\beta\epsilon} + 2e^{-4\beta\epsilon}} = \frac{e^{-2\beta\epsilon}}{Q}$$

sigmoidal transition

reminiscent of real
protein denaturation

*Adapted from Physical Biology of
the Cell (Chapter 8)*

Identification of protein-like (foldable) structures

structure	sequence						no. of sequences
	1	2	3	4	5	6	
	○	●	○	⊗	●	⊗	9
	○	●	●	⊗	●	○	
	●	●	⊗	○	●	○	
	●	●	○	○	●	●	
	○	○	●	⊗	⊗	●	6
	○	●	●	⊗	○	●	
	●	○	○	●	⊗	●	3
	●	●	○	●	○	●	

enumerate all 64 possible protein configurations

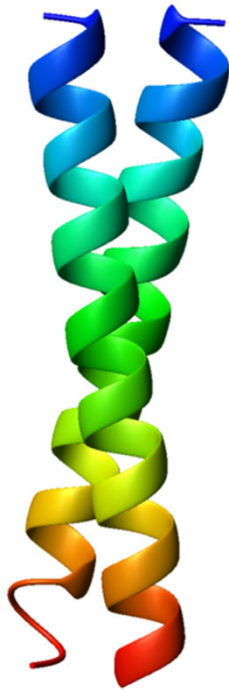
→ determine energy of each

necessary pre-requisite for a stable fold: at least one HH contact

The "hairpin" is the most designable structure

→ simple models like this: **Protein design principles**

Real structures: Simple tertiary structure motifs



GCN4 coiled coil domain
PDB: 1zik

Secondary structure elements form the **elementary motifs** of protein structure.

Quiz:

The sequence of GCN4 is given as follows:
RMKQLEDKVEELLSKNYHLENEVARLKKLVGER

how can it be immediately recognized that this folds into a coiled coil?

Helix bundles: Inherently designable structures



Hecht et al. Protein Sci 2004

Secondary structure

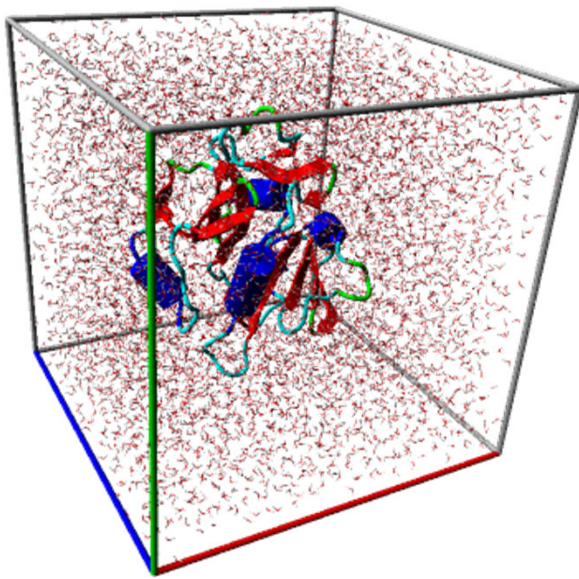
→ fixed, helical

Tertiary structure:

follows HP rules

Provides a platform, on which further functionality can be designed

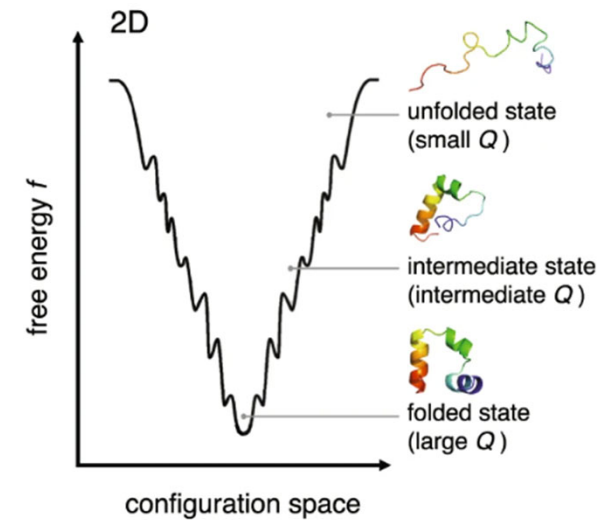
Force field for protein structure



<https://in.explara.com/>

Force field for protein structure evaluation:

$$\begin{aligned}
 V = & \sum_{bonds} a_{\alpha} (x_i - x_{i0})^2 \\
 & + \sum_{bond \text{ angles}} b\beta (\theta_i - \theta_{i0})^2 \\
 & + \sum_{charges} \frac{Z_i Z_j e^2}{D(r) r_{ij}} \\
 & + \sum_{neutral \text{ atoms}} 4d_{\delta} \left[\left(\frac{A i_j}{r i_j} \right) 12 - \left(\frac{B_{ij}}{r_{ij}} \right) \right]
 \end{aligned}$$

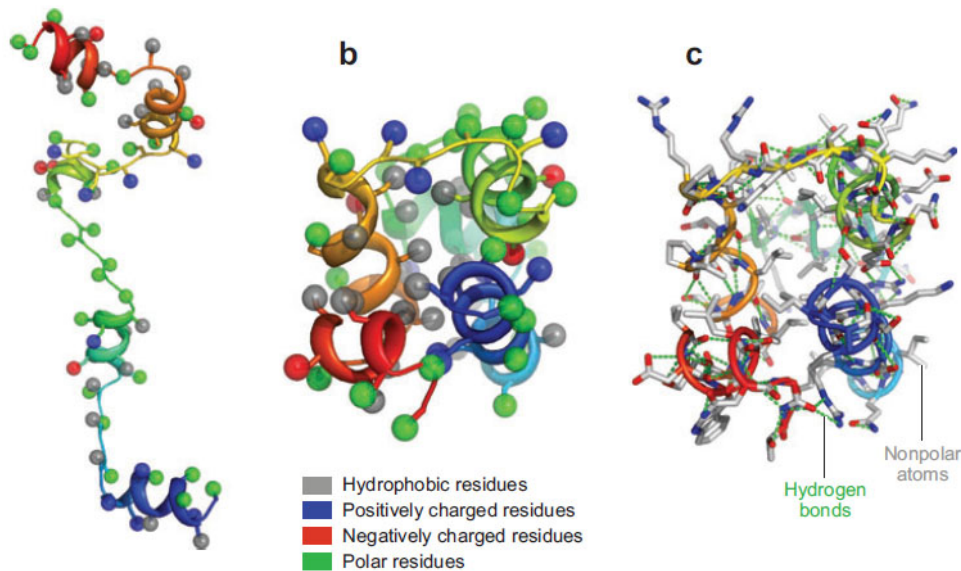


<https://www.nature.com/articles/s41598-019-50825-6>

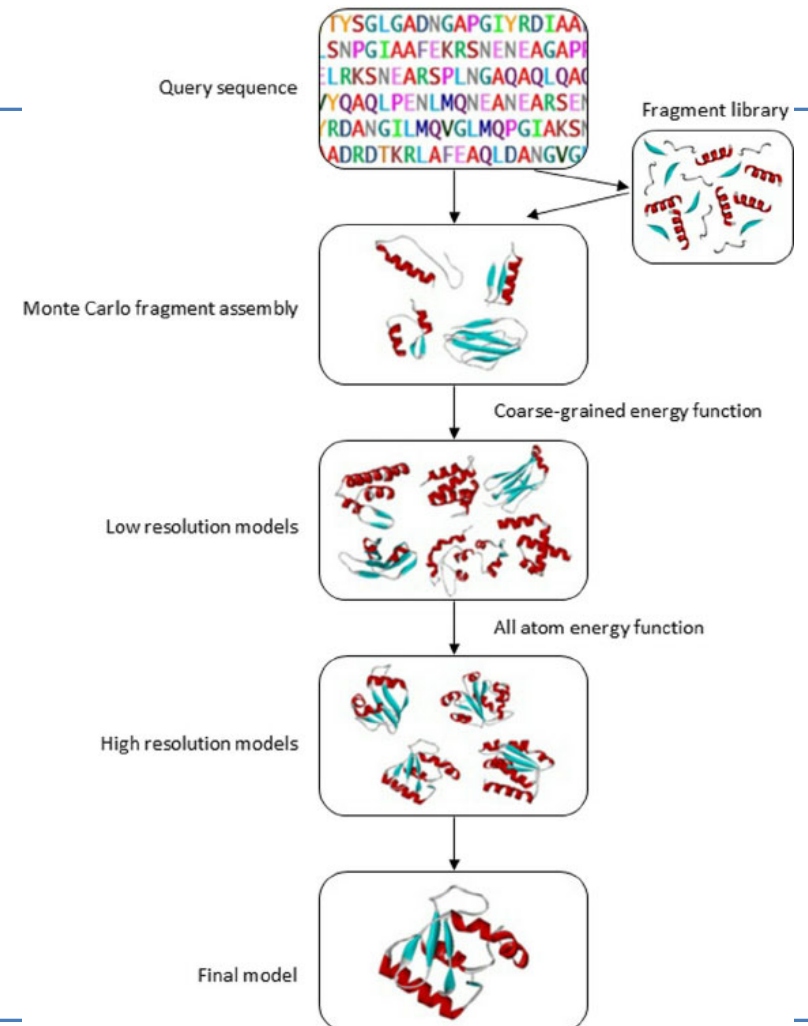
Goal: Minimize the configurational energy, find the global minimum

Protein structure prediction / design

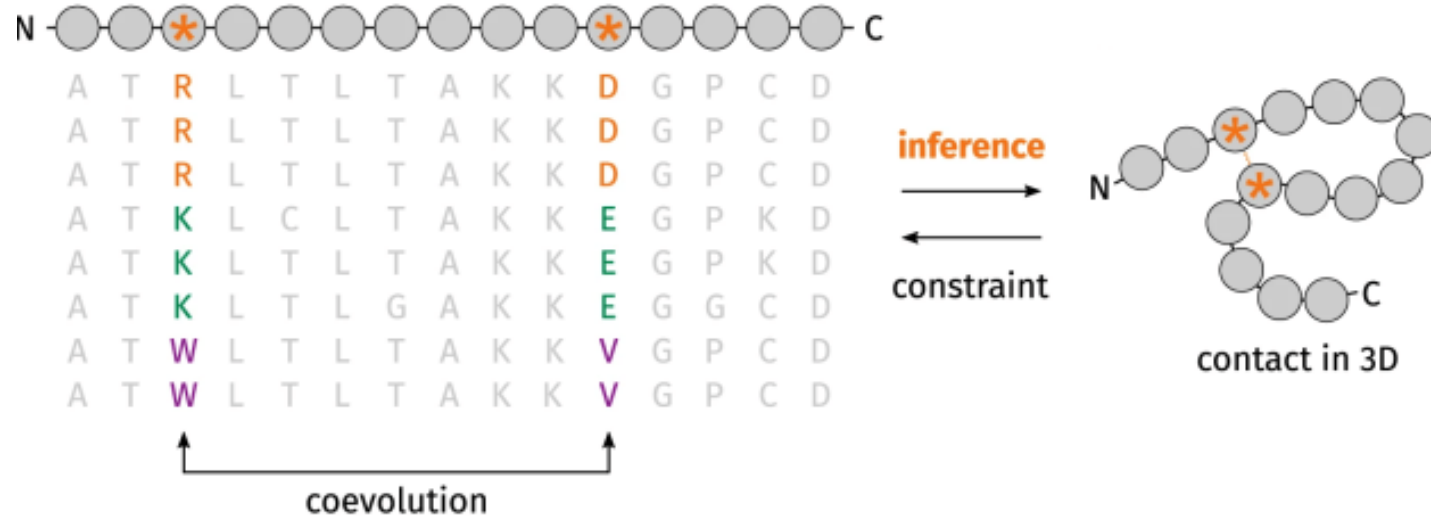
Design from fragment libraries,
followed by refinement (Rosetta)



Das & Baker, Annu Rev Biochem 2008

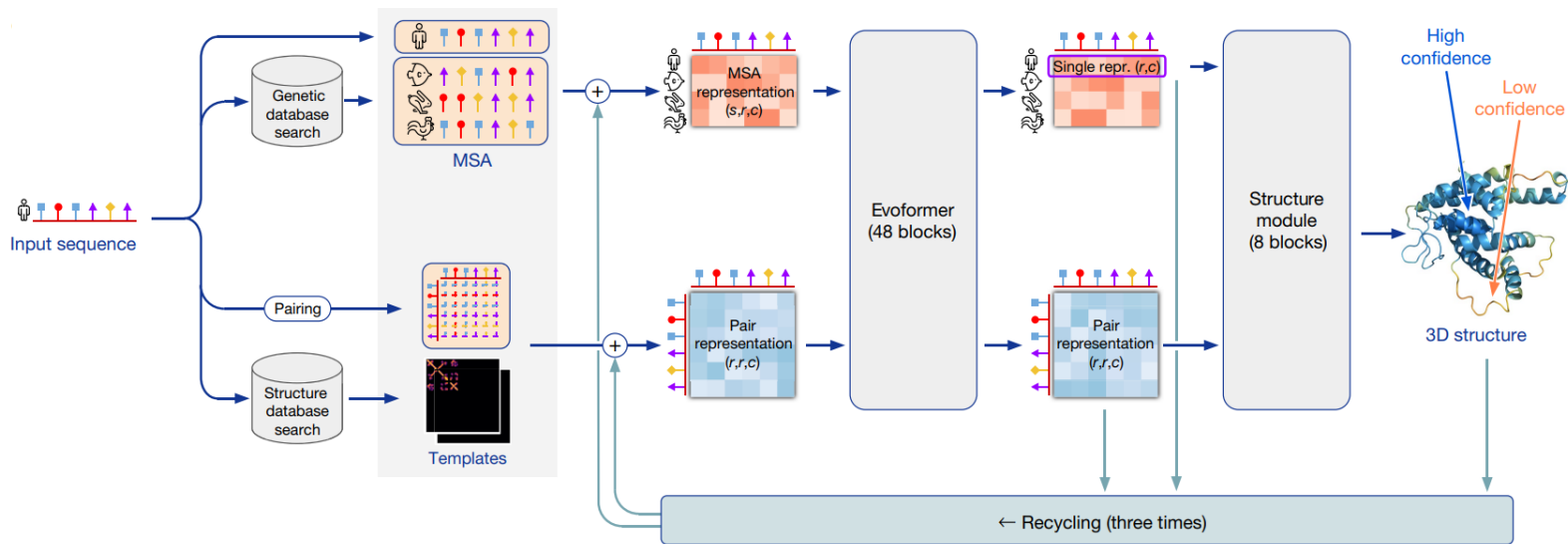


Structural information from sequence: Co-evolution analysis



[43146:42rxuqdsrqhB35;:99](#)

Protein structure prediction – ML approaches



Input:

- primary sequence of target protein
- multiple sequence alignments of homologues
- structural information of homologues (PDB)

Process 1:

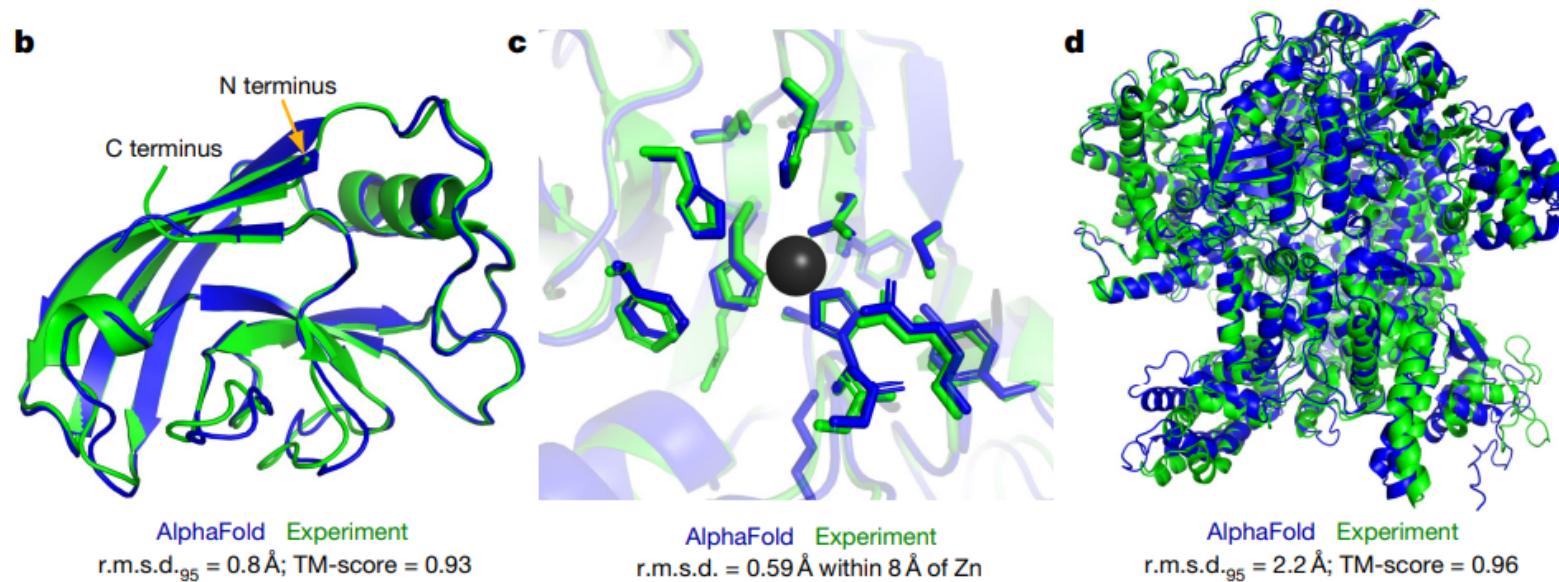
- MSA representation
- Residue pair representation

Process 2:

- 3D structure representation: rotation & translation of each residue
- refinement

AlphaFold2 - Nature 2021

Protein structure prediction – ML approaches

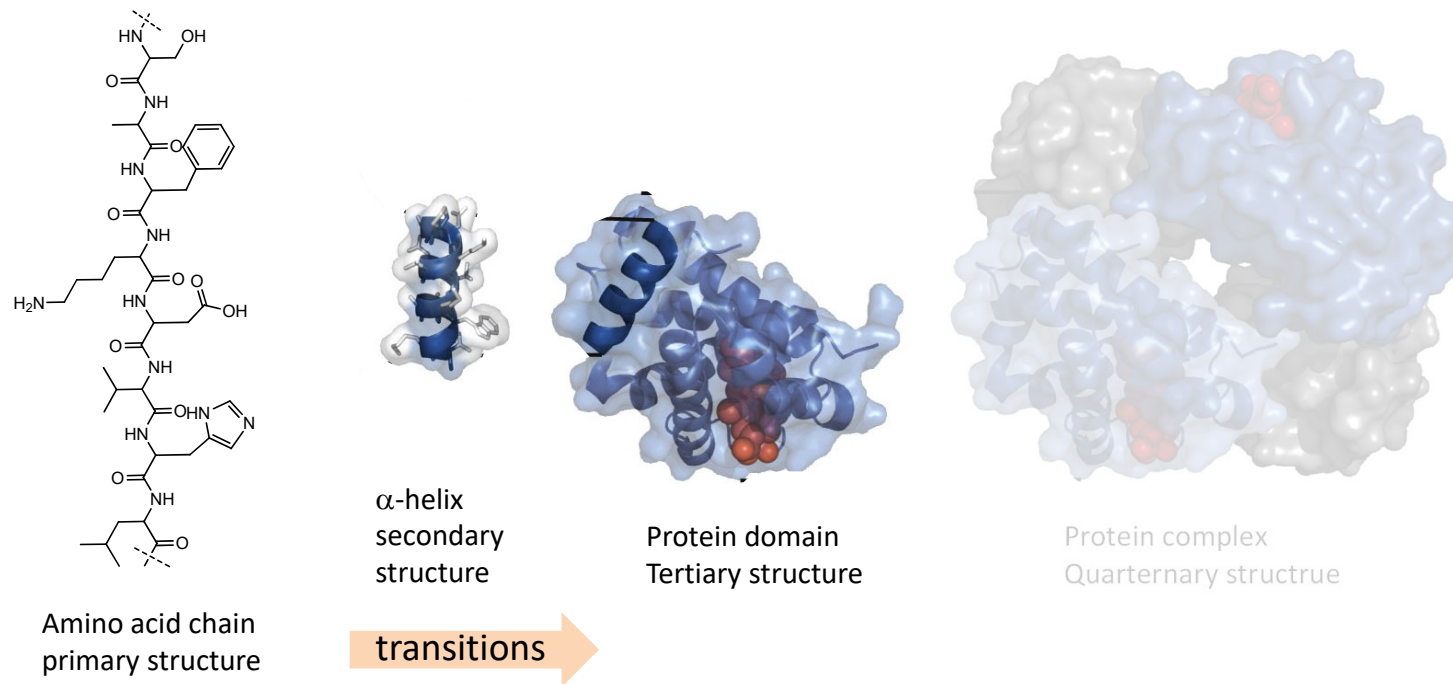


Result:

- highly accurate structure prediction
- low backbone RMSD
- correct residue orientation

AlphaFold - Nature 2021

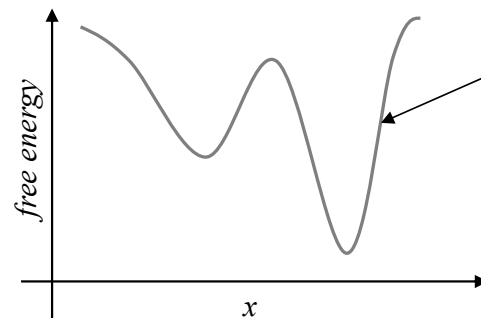
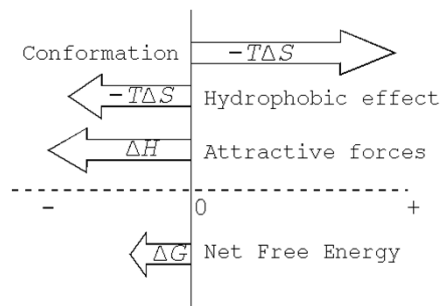
Protein structure – A thermodynamic view



A free energy surface to understand protein structure

using a basic chemistry principles, **the free energy surface**, to describe state transitions in proteins

Free energy:



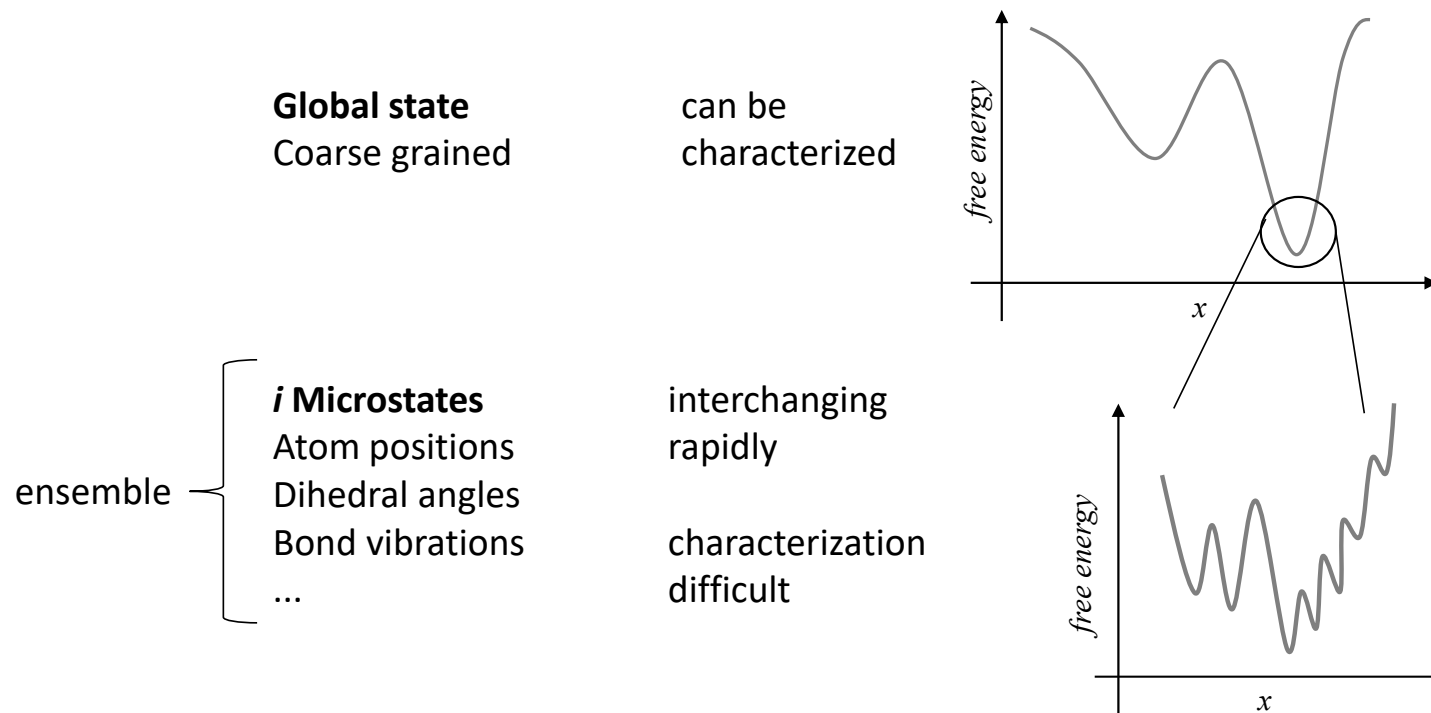
each (populated) protein conformation falls somewhere on this line

some reaction coordinate:

- solvent accessibility
- compactness
- % hydrogen bonds saturated

Global states in proteins

For a biophysical understanding → simplifications are required.



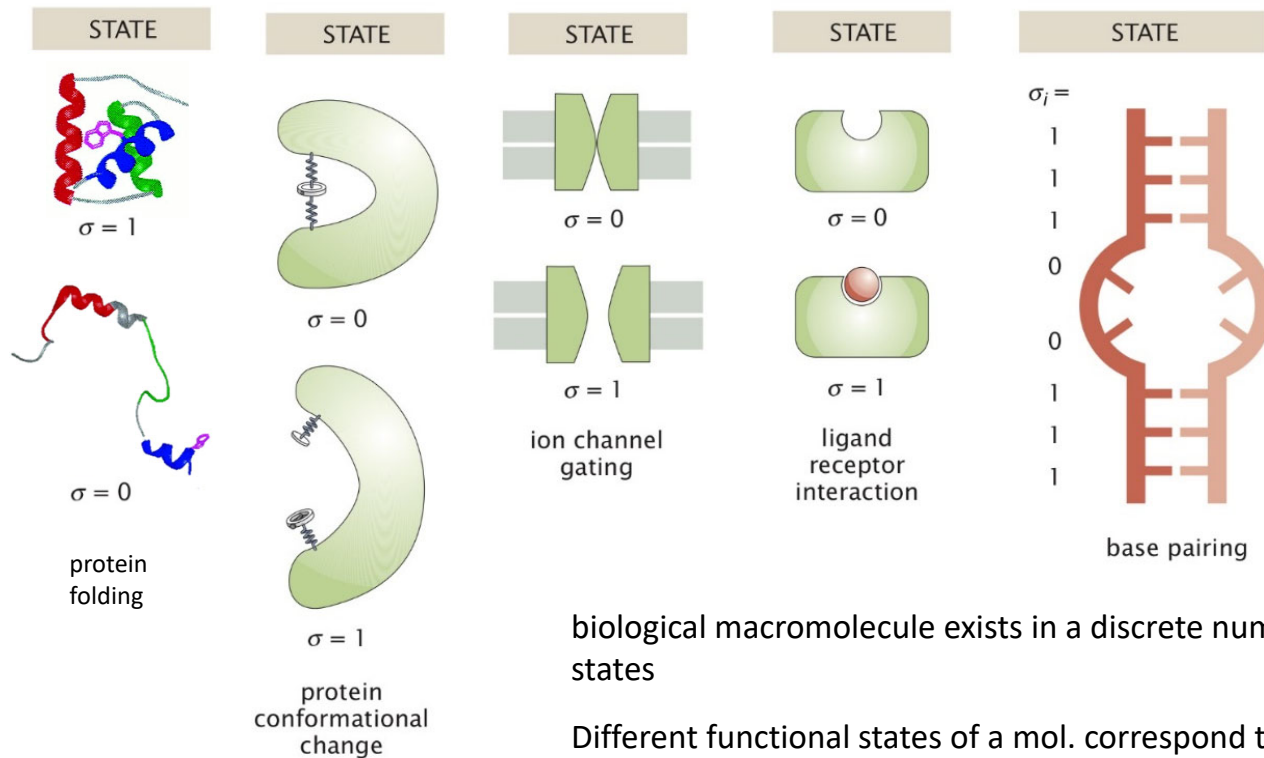
Global states in proteins

Biology: Global states are useful concept

- We can assume that any biological macromolecule exists in a discrete number of global states, dependent e.g. on the environment
- Different functional states of a protein correspond to different global states
- Changes in global states could be related to function

As discussed earlier, complex systems such as proteins can be treated with **statistical thermodynamics**: This allows to extract useful parameters.

Motivation – biomolecules exist in multiple states

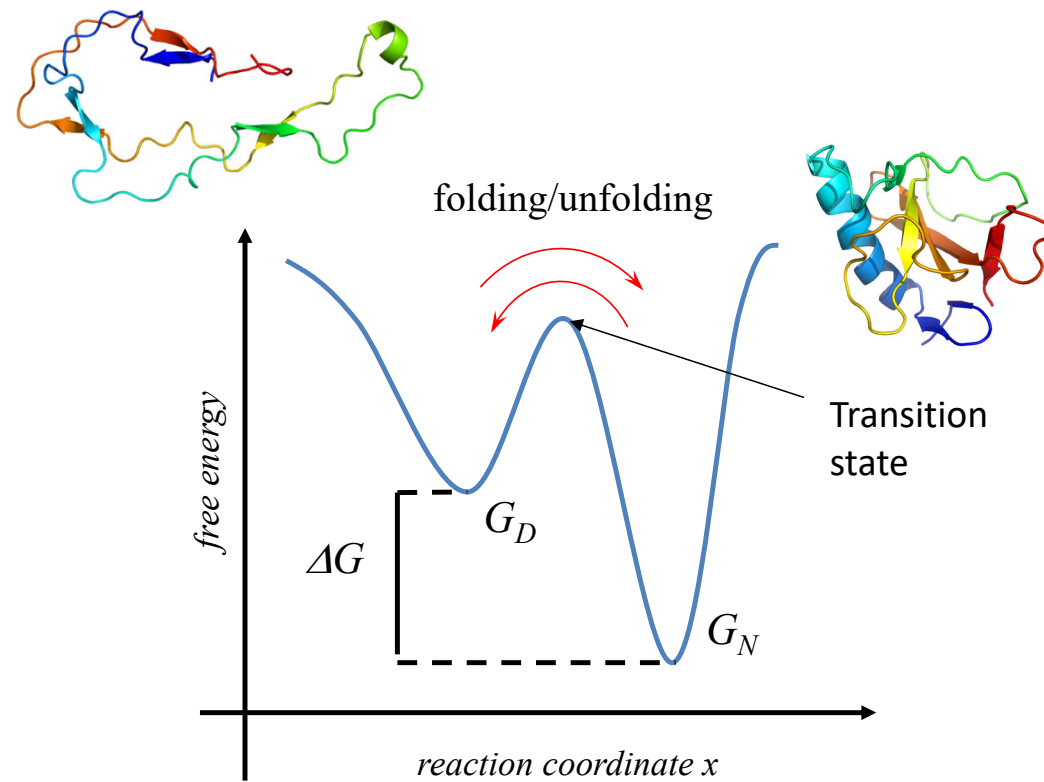


biological macromolecule exists in a discrete number of global states

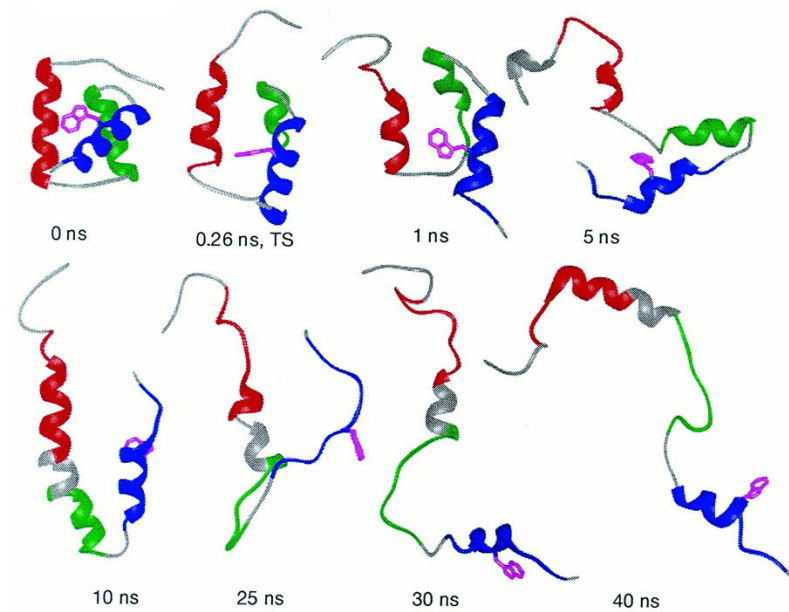
Different functional states of a mol. correspond to different global states

Changes in global states could be related to function

Global states in a protein: N and D



Protein denaturation process



Mayor & Fersht, PNAS 2000

can be reversible:

- Loss of defined tertiary structure
- Partial loss / change in secondary structure
- exposure of buried hydrophobic amino acids

or irreversible

- at high protein concentration, aggregation
- can make sick (prions)

→ unfolding eq.

How can we observe two-state transitions?

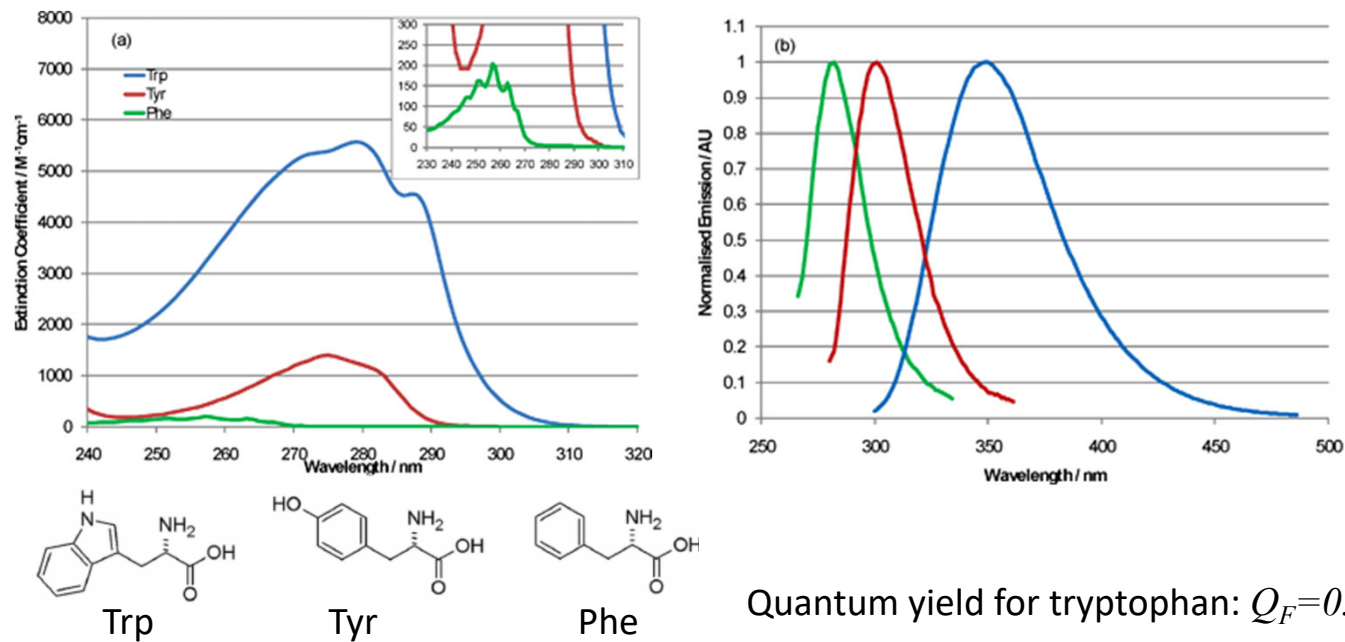
Any methods that can distinguish between U and N

- **Absorbance** (e.g. Trp, Tyr) due to change in the micro-environment
- **Fluorescence** (Trp)-difference in emission spectrum & intensity, due to change in microenvironment
- **Circular dichroism** (far or near UV), due to change in asymmetric environment of fluorophores
- **Calorimetry** (DSC), due to change in heat capacity and heat absorption
- **NMR spectroscopy**
- **Gel electrophoresis** or **size exclusion chromatography**
- **Catalytic activity**, functional assays
- **External probes** (chromophores, fluorophores)

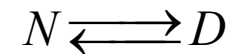
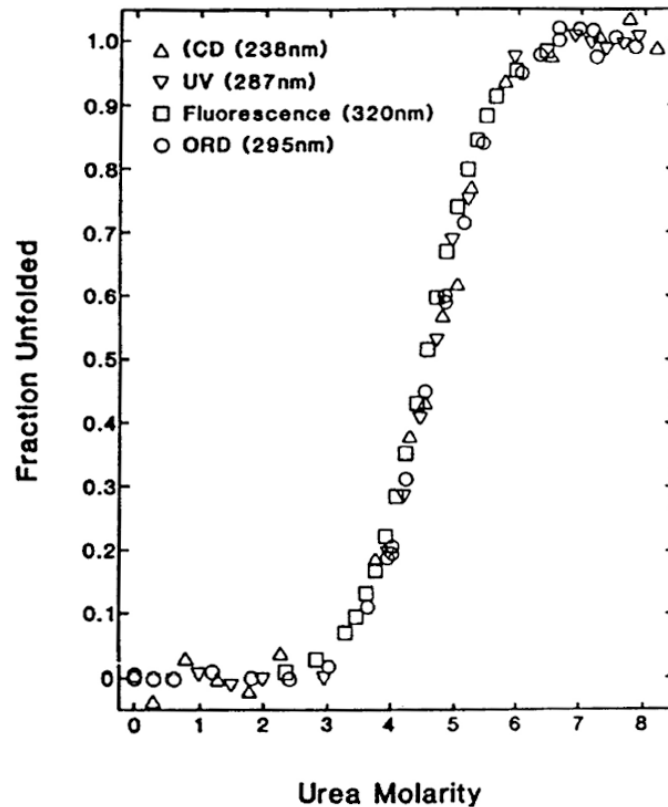
→ fluorescence

Amino acids: Fluorescence spectra

Absorbance and fluorescence spectra of aromatic amino acids



Denaturation of globular, monomeric protein : RNase T1



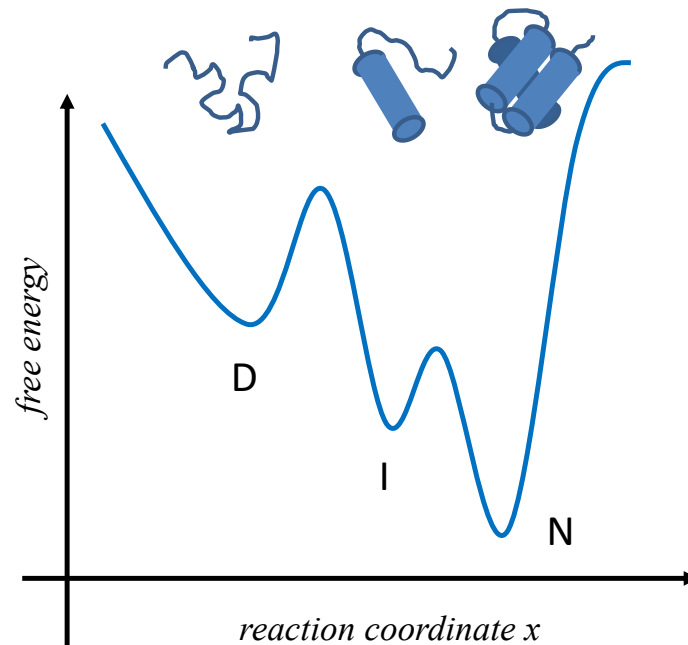
$$y = [N]y_N + [D]y_D$$

$$K_D = \frac{[D]}{[N]} = \frac{y_N - y}{y - y_D}$$

different parameters completely overlap

normalized transitions ($\theta_N = [N] / ([N] + [D])$) overlap

Three (or more) state equilibrium transitions

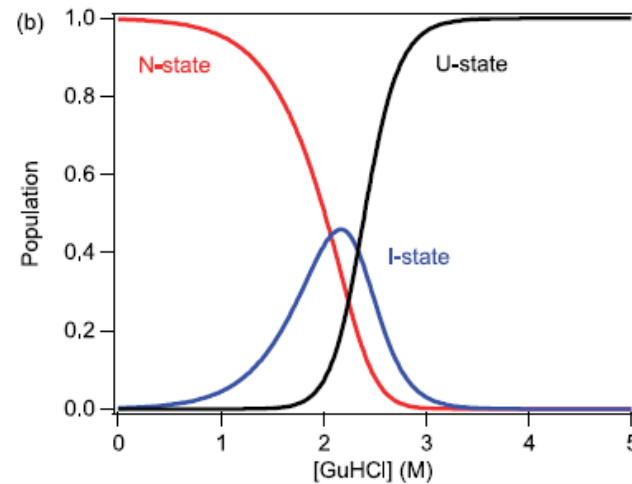
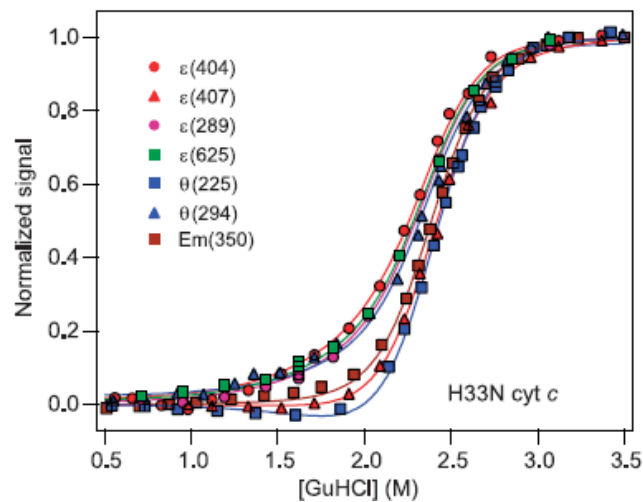


In many proteins, intermediates are populated.

Intermediates include proteins, where only partial structure has formed.

This complicates the analysis.

Multistate transitions in cytochrome c unfolding

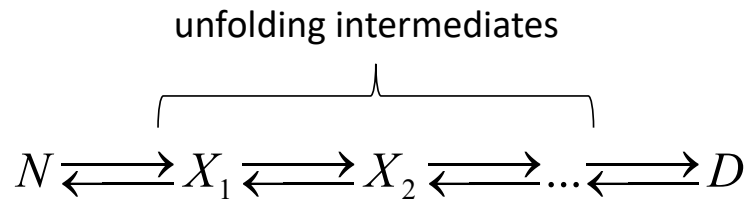


Latypov et al.
JMB 2006

If different parameters are observed, unfolding traces do no longer coincide.

Intermediates accumulate during the unfolding transition

Multi-state transition



apparent stability, elucidated
by summing the individual
contributions

$$K_{app} = K_D \frac{1 + \sum d_i \frac{K_i}{K_D}}{1 + \sum (1 - d_i) K_i} = \frac{K_D + \sum d_i K_i}{1 + \sum (1 - d_i) K_i}$$

$$d_i = \frac{y_i - y_N}{y_D - y_N}, \quad 0 < d_i < 1$$

$$K_i = \frac{[X_i]}{[N]} \quad K_D = \frac{[D]}{[N]}$$

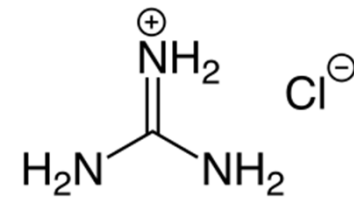
Denaturation with chemical agents

Molecular mechanism of denaturant action:

1. Direct effect:

H-bonding to polar groups, mostly the protein backbone, thereby competing with internal H-bonds

If charged: Interaction with ionic groups

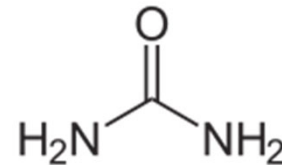


guanidinium
chloride

2. Indirect effect:

Alteration of water structure and thus diminishment of the hydrophobic effect

Facilitation of the exposure of hydrophobic groups.



urea

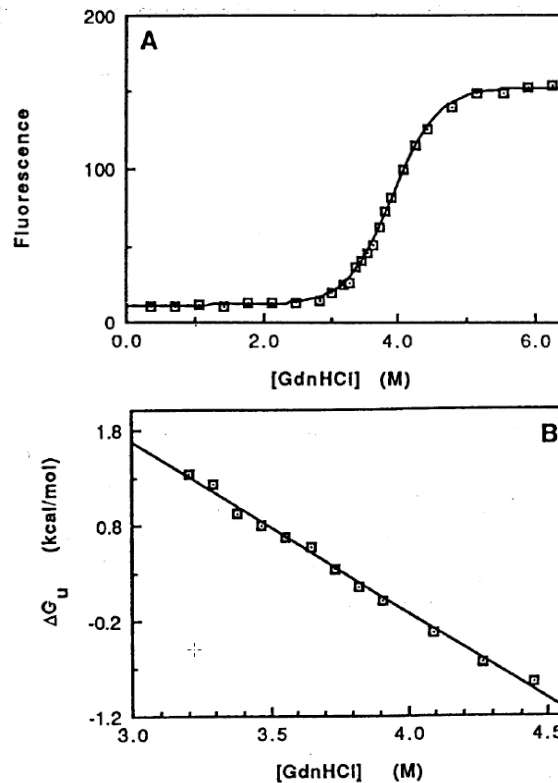
Protein denaturation with denaturants

The **effect of denaturants** on the free energy is linear (empirical finding)

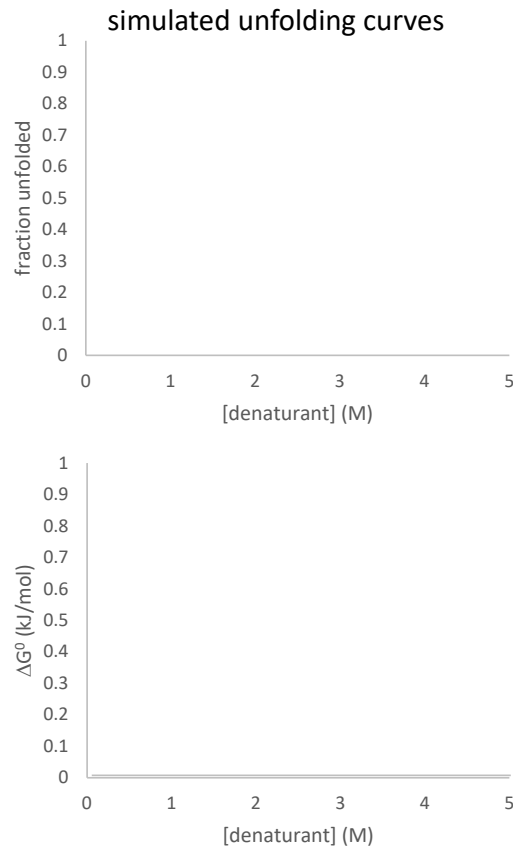
$$\Delta G^0 = \Delta G_{H_2O}^0 + m [\text{denaturant}]$$

The **free energy of unfolding** can thus be determined by an extrapolation to **0 M denaturant**

Example: Chymotrypsin inhibitor 2 (CI2)



Sensitivity to denaturant



Parameters

— $\Delta G_0 = -40 \text{ kJ/mol}$, $m = 18 \text{ kJ/mol/M}$

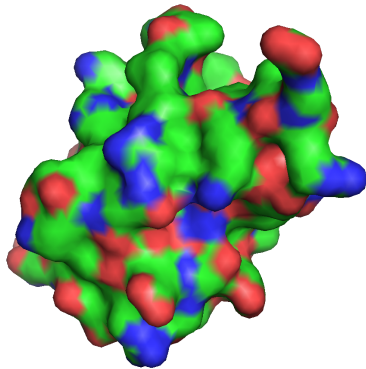
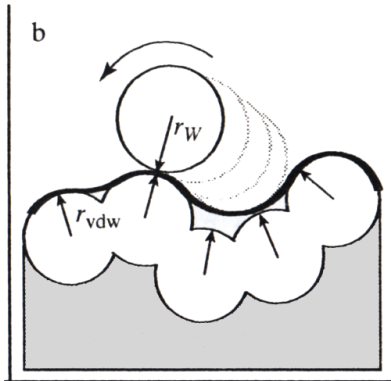
— $\Delta G_0 = -26.5 \text{ kJ/mol}$, $m = 12 \text{ kJ/mol/M}$

— $\Delta G_0 = -13.1 \text{ kJ/mol}$, $m = 6 \text{ kJ/mol/M}$

molecular meaning of m-value:

- proportional of buried ASA
- proteins with large hydrophobic core exhibit high m-value
- the higher the m-value the stronger the dependence of a folding transition to denaturant (steepness)

M-values are proportional to change in ASA



Calculating ASA

- a water-sized sphere is rolled across the chemical structure keeping VdW radii
- the accessible surface corresponds to the ASA

molecular meaning of m-value:

- proportional to change in ASA
- proteins with large hydrophobic core exhibit high m-value
- the higher the m-value the stronger the dependence of a folding transition to denaturant (steepness)

Small quiz:

- We have a small protein, whose standard free energy of folding (stability) is $\Delta G_f^\circ = 20 \text{ kJ/mol}$
- Upon addition of guanidinium hydrochloride (GdmHCl), the protein denatures reversibly
- Fluorescence measurements determined a mid-point of the transition at 2 M GdmHCl
- What is the *m-value* for this protein?
- If we compare this to a different protein with $m = 5 \text{ kJ/mol/M}$, what can we say about its structure?